## 2008 AP® CALCULUS AB FREE-RESPONSE QUESTIONS

- 3. Oil is leaking from a pipeline on the surface of a lake and forms an oil slick whose volume increases at a constant rate of 2000 cubic centimeters per minute. The oil slick takes the form of a right circular cylinder with both its radius and height changing with time. (Note: The volume V of a right circular cylinder with radius r and height h is given by  $V = \pi r^2 h$ .)
  - (a) At the instant when the radius of the oil slick is 100 centimeters and the height is 0.5 centimeter, the radius is increasing at the rate of 2.5 centimeters per minute. At this instant, what is the rate of change of the height of the oil slick with respect to time, in centimeters per minute?
  - (b) A recovery device arrives on the scene and begins removing oil. The rate at which oil is removed is  $R(t) = 400\sqrt{t}$  cubic centimeters per minute, where t is the time in minutes since the device began working. Oil continues to leak at the rate of 2000 cubic centimeters per minute. Find the time t when the oil slick reaches its maximum volume. Justify your answer.
  - (c) By the time the recovery device began removing oil, 60,000 cubic centimeters of oil had already leaked. Write, but do not evaluate, an expression involving an integral that gives the volume of oil at the time found in part (b).

WRITE ALL WORK IN THE PINK EXAM BOOKLET.

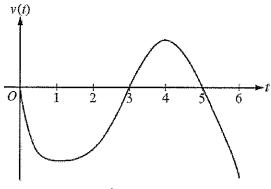
**END OF PART A OF SECTION II** 

## 2008 AP® CALCULUS AB FREE-RESPONSE QUESTIONS

CALCULUS AB
SECTION II, Part B

Time—45 minutes
Number of problems—3

No calculator is allowed for these problems.



Graph of v

- 4. A particle moves along the x-axis so that its velocity at time t, for  $0 \le t \le 6$ , is given by a differentiable function v whose graph is shown above. The velocity is 0 at t = 0, t = 3, and t = 5, and the graph has horizontal tangents at t = 1 and t = 4. The areas of the regions bounded by the t-axis and the graph of v on the intervals [0, 3], [3, 5], and [5, 6] are 8, 3, and 2, respectively. At time t = 0, the particle is at x = -2.
  - (a) For  $0 \le t \le 6$ , find both the time and the position of the particle when the particle is farthest to the left. Justify your answer.
  - (b) For how many values of t, where  $0 \le t \le 6$ , is the particle at x = -8? Explain your reasoning.
  - (c) On the interval 2 < t < 3, is the speed of the particle increasing or decreasing? Give a reason for your answer.
  - (d) During what time intervals, if any, is the acceleration of the particle negative? Justify your answer.

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